

CreutzFest 2014

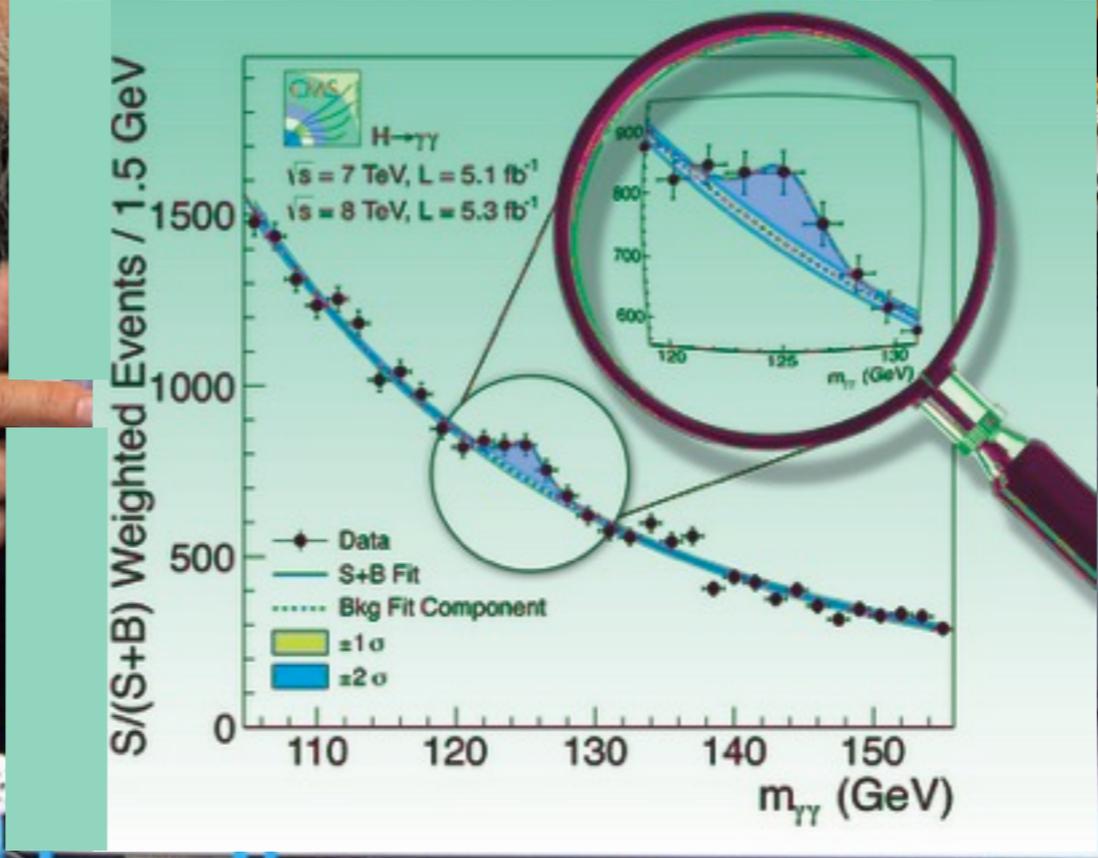
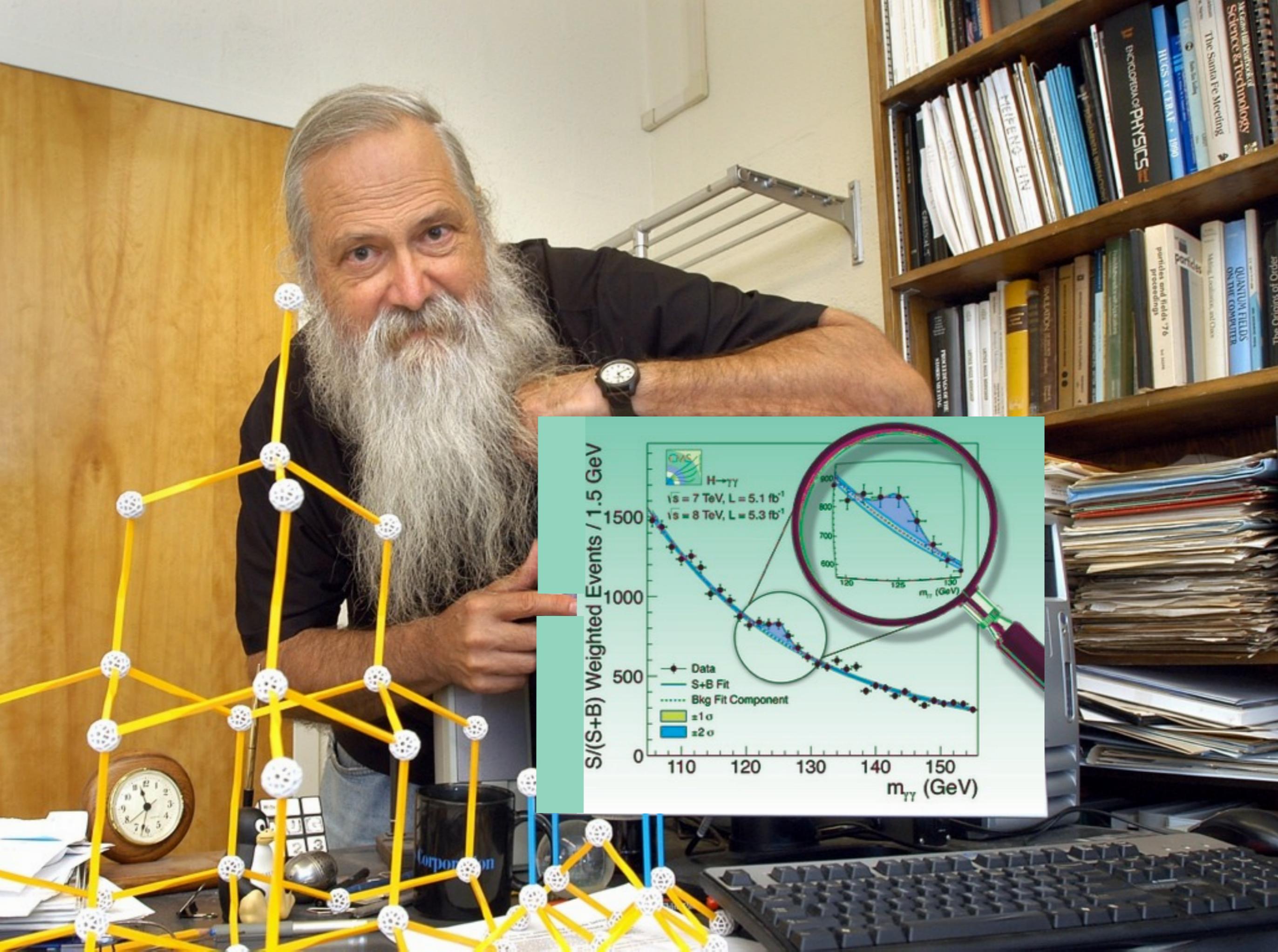
# From Mike to the Higgs impostor and the dilaton

**Julius Kuti**

University of California, San Diego

**Creutz Fest 2014**

**BNL, September 4-5, 2014**



# Outline

## Mike's impact on my early lattice work

two seminal papers in 1979: Creutz and Wilson  
1979-80: first lattice work after off-lattice frustration  
the story of the first QCD simulation in Hungary

## What is the composite Higgs?

searching the needle in the haystack?  
or, searching for the haystack?

## The sextet model and the toolset

low mass scalar emerging  
resonance spectrum  $\sim 2$  TeV range  
running coupling  
spectral density and chiral condensate

## Early universe

EW phase transition  
dark matter

## Summary and Outlook

The quark-nucleon phase diagram and quantum chromodynamics

J. Kuti, B. Lukács, J. Polónyi, K. Szlachányi

Abstract

The temperature dependence of a conjectured first-order phase transition between nuclear matter and quark-gluon matter is calculated for temperatures below  $T = 200$  MeV. On the nuclear side a rather successful meson-nucleon mean field theory is applied while quark-gluon matter at large densities and finite temperatures is described perturbatively by quantum chromodynamics. Outside the finite volume of hot and dense quark-gluon matter the physical vacuum is characterized, by the newly determined bag parameter  $\Lambda_B = 235$  MeV. We observe a dramatic drop in the density of nuclear matter at the phase transition point as the temperature increases, if the scale parameter  $\Lambda$  of QCD is chosen as  $\Lambda = 100$  MeV. For larger values of  $\Lambda$  the effect is less pronounced. Further work is required to settle this problem.

1979 : frustrations to describe the QCD phase transition

Two seminal papers appear in preprint form in 1979: Mike is on both

After reading Mike's string tension result I knew what to do

How on earth can I do a lattice simulation in Hungary in 1979?

the iPhone today would beat the R40 russian "supercomputer" Hungary had (with 1 MB disk storage for research institute where I worked at that time) broke down every few hours, served several hundred researchers

Early 1980: Hungarian National Academy buys and IBM 3030 computer (like a VAX 780)

U.S. Congress sets condition: no atomic or nuclear research on the machine and particle physics is nuclear

Dubna-CERN deep-inelastic muon experiment with strong group from Hungary  
They cannot use the badly needed computer either - experiment is East-West poster child  
Van Hove (DG of CERN) comes to Hungary to convince Academy and IBM office to ask for US congressional exception for the experiment

remaining condition: IBM rep will check computer output every night

There we go “doing the muon experiment” and outputting in the lattice Monte Carlo some phony lines: “now we are calculating muon scattering at 5 degrees ...”

trouble: IBM reps notices that this angle was already calculated (oh my, the real experimental group had real scattering at real angles printed the previous night)

We find the phase transition before I board the plane for Madison, Wisconsin (ICHEP 1980)

Roman Jackiw gives me 10 minutes to talk in the session and Mike lists the result in the crowded room of his talk as part of the first QCD applications emerging

# Thank you Mike for showing the way and fueling the excitement!

## MONTE CARLO STUDY OF SU(2) GAUGE THEORY AT FINITE TEMPERATURE

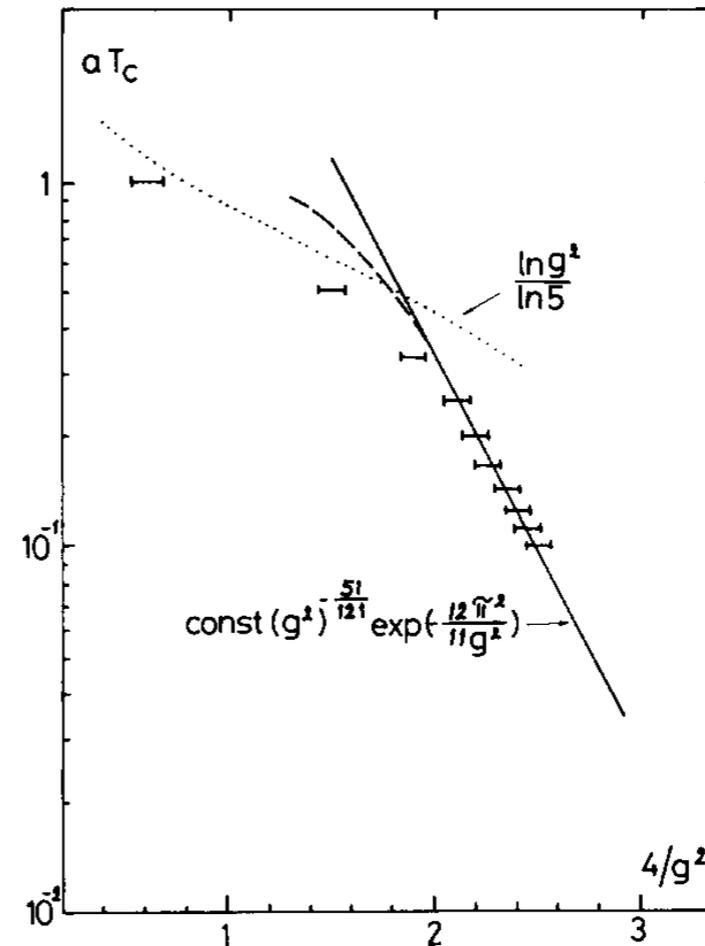
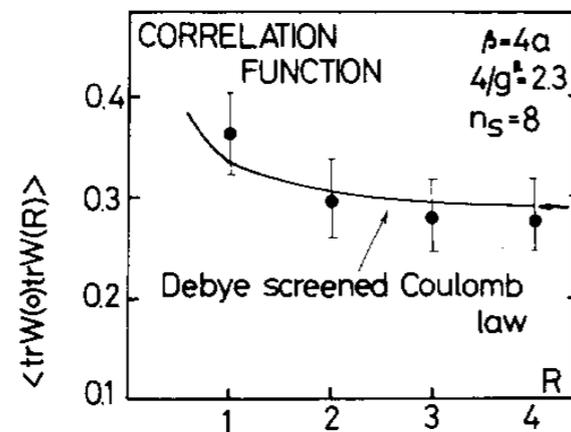
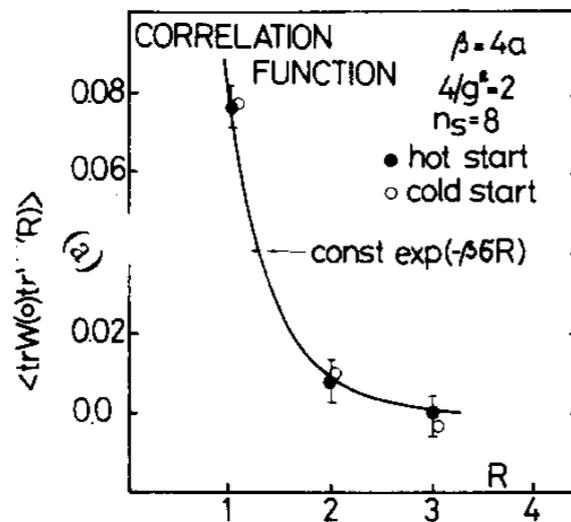
J. KUTI, J. POLÓNYSI and K. SZLACHÁNYI

Central Research Institute for Physics, H-1525 Budapest, Hungary

Received 9 September 1980

We find numerical evidence for the phase transition between the confinement phase and free Coulomb phase of SU(2) Yang–Mills theory with lattice cut-off. The search for the critical temperature is based on a Monte Carlo study of the string tension between a heavy  $Q\bar{Q}$ -pair in a heat bath. The arbitrary normalization  $0.2 \text{ GeV}^2$  is used for the string tension at zero temperature when a smooth extrapolation of the lattice theory to the continuum limit is carried out. Our numerical estimate for the critical temperature is  $T_c \approx 160 \pm 30 \text{ MeV}$  in the absence of quark degrees of freedom. It is suggested that the phase transition is of second-order.

important scale setting  
Hasenfratz<sup>2</sup>

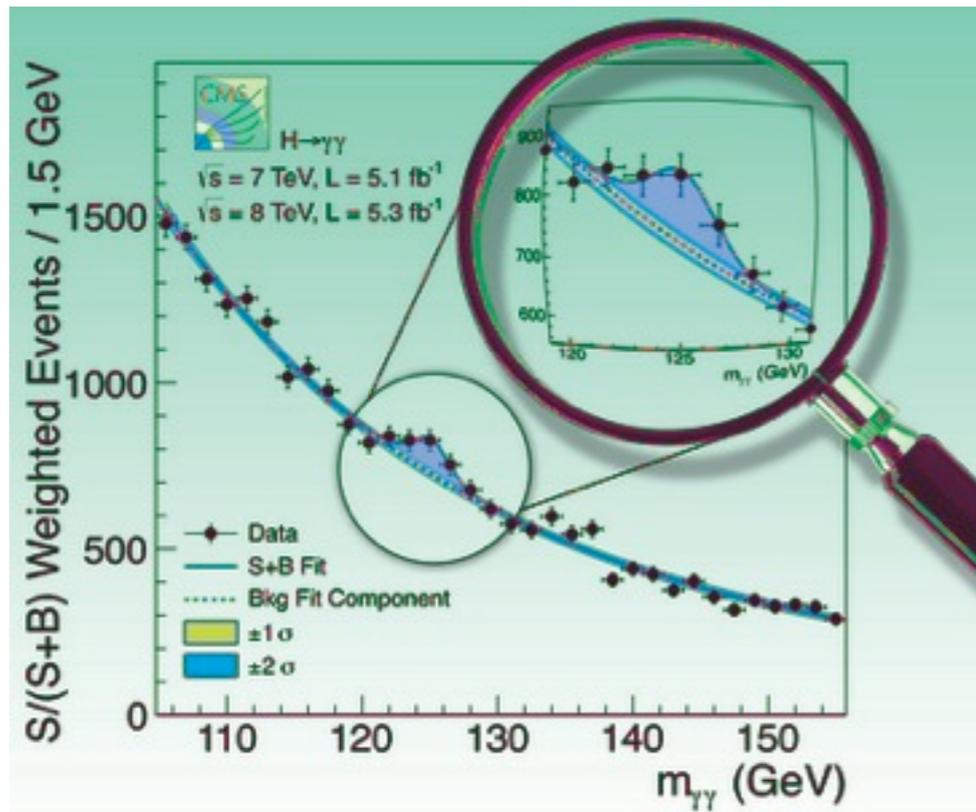


# onto the Higgs

Lattice Higgs Collaboration ( $L_{\text{at}}\text{HC}$ )

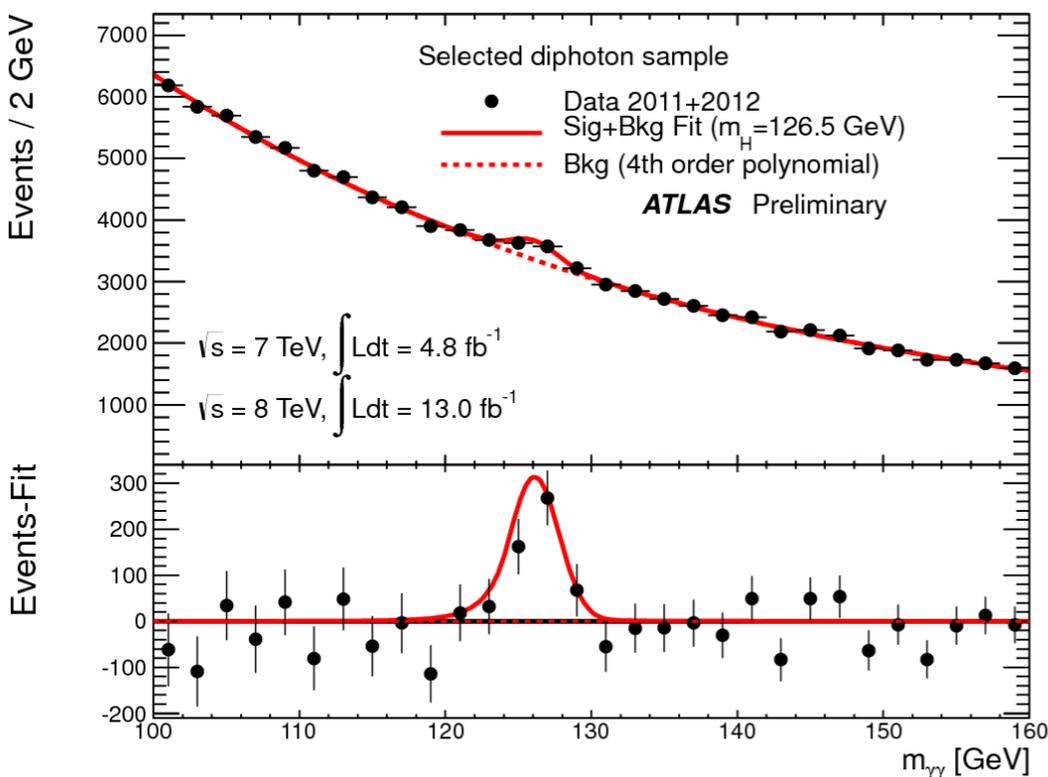
Zoltan Fodor, Kieran Holland, Santanu Mondal, Daniel Nogradi, Chik Him Wong

# Rational for lattice BSM?



**voices:** a light Higgs-like scalar was found, consistent with SM within errors, and composite states have not been seen below 1 TeV. Strongly coupled BSM gauge theories are Higgs-less with resonances below 1 TeV

**facts:** Compositeness has not been shown to be incompatible with the light Higgs scalar; earlier search for compositeness was based on naively scaled up QCD and unacceptable old technicolor guessing games. Resonances, out of first LHC run reach, are in the 2-3 TeV range in the theory I will discuss



**lattice BSM plans:** LHC14 run will search for new physics from compositeness and SUSY, and the lattice BSM community is preparing quantitative lattice based predictions to be ruled in or ruled out.

# What is the composite Higgs mechanism?

the Higgs doublet field

$$H = \frac{1}{\sqrt{2}} \begin{pmatrix} \pi_2 + i\pi_1 \\ \sigma - i\pi_3 \end{pmatrix} = \frac{1}{\sqrt{2}} (\sigma + i\vec{\tau} \cdot \vec{\pi}) \equiv M$$

$$D_\mu M = \partial_\mu M - ig W_\mu M + ig' M B_\mu, \quad \text{with} \quad W_\mu = W_\mu^a \frac{\tau^a}{2}, \quad B_\mu = B_\mu \frac{\tau^3}{2}$$

The Higgs Lagrangian is

**spontaneous symmetry breaking**  
**Higgs mechanism**

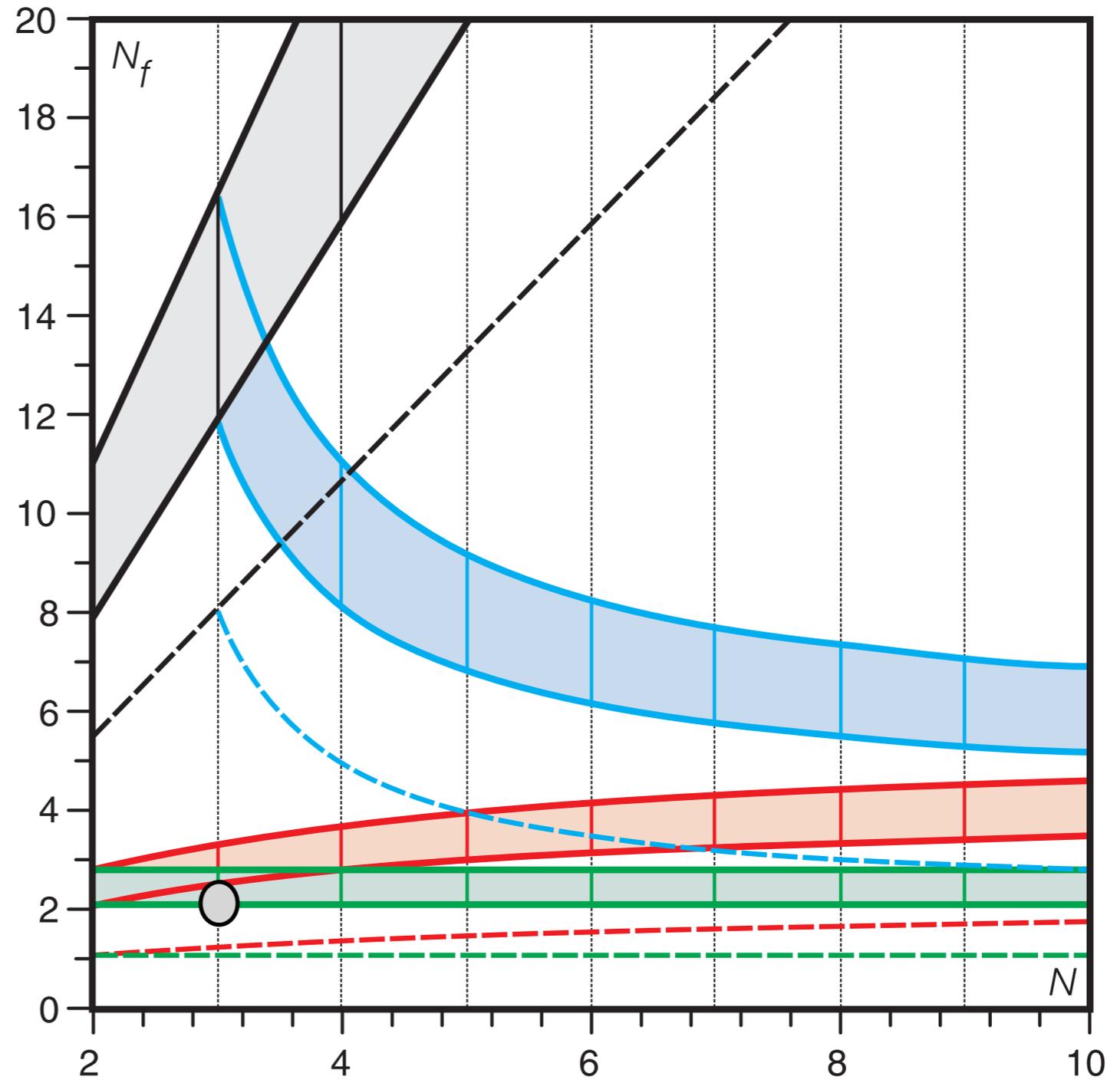
$$\mathcal{L} = \frac{1}{2} \text{Tr} [D_\mu M^\dagger D^\mu M] - \frac{m_M^2}{2} \text{Tr} [M^\dagger M] - \frac{\lambda}{4} \text{Tr} [M^\dagger M]^2$$

$$\mathcal{L}_{Higgs} \rightarrow -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{Q}\gamma_\mu D^\mu Q + \dots$$

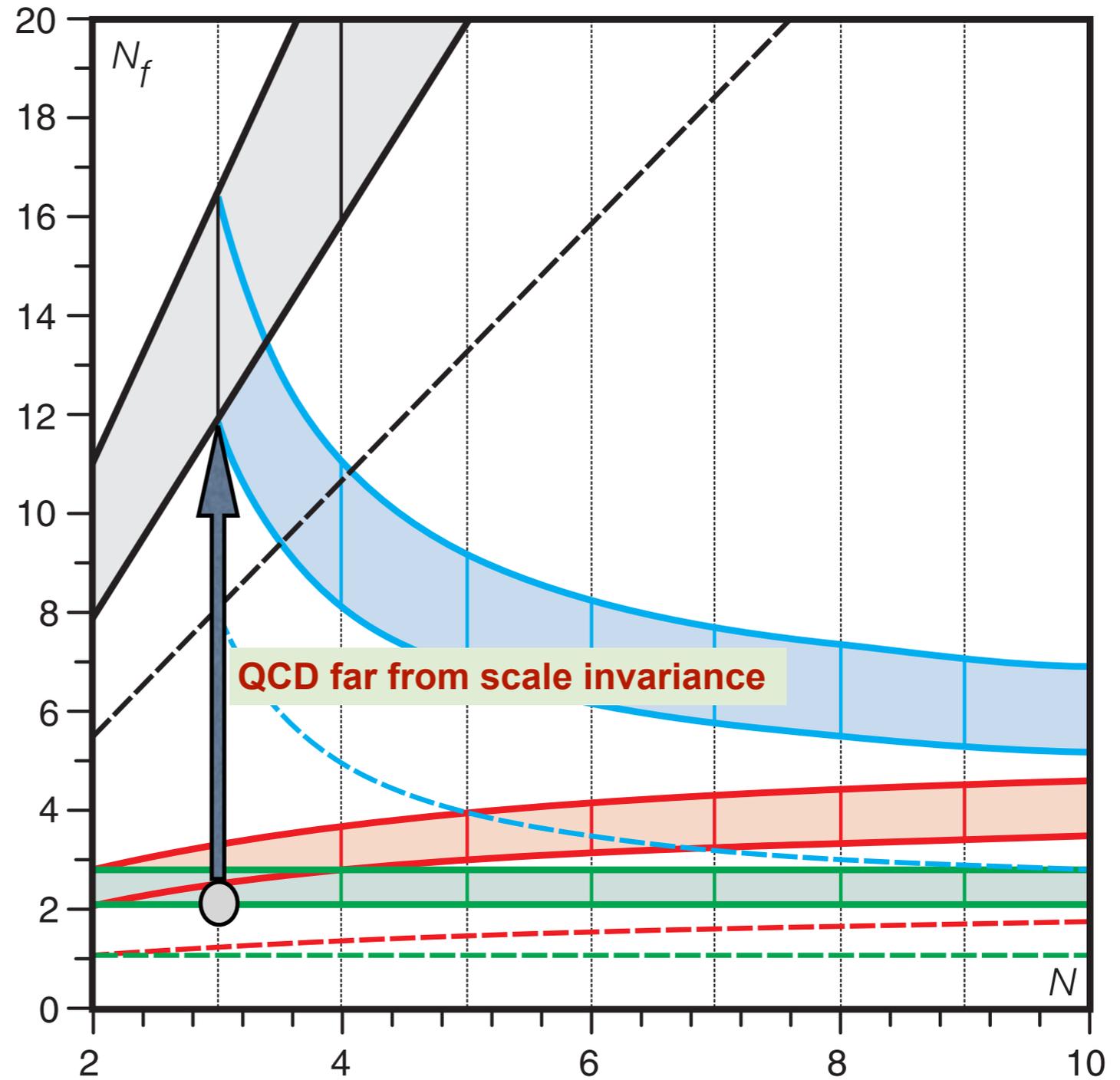
**strongly coupled gauge theory**  
**fermions (Q) in gauge group reps**

**needle in the haystack?**  
**or, just one of the haystacks?**

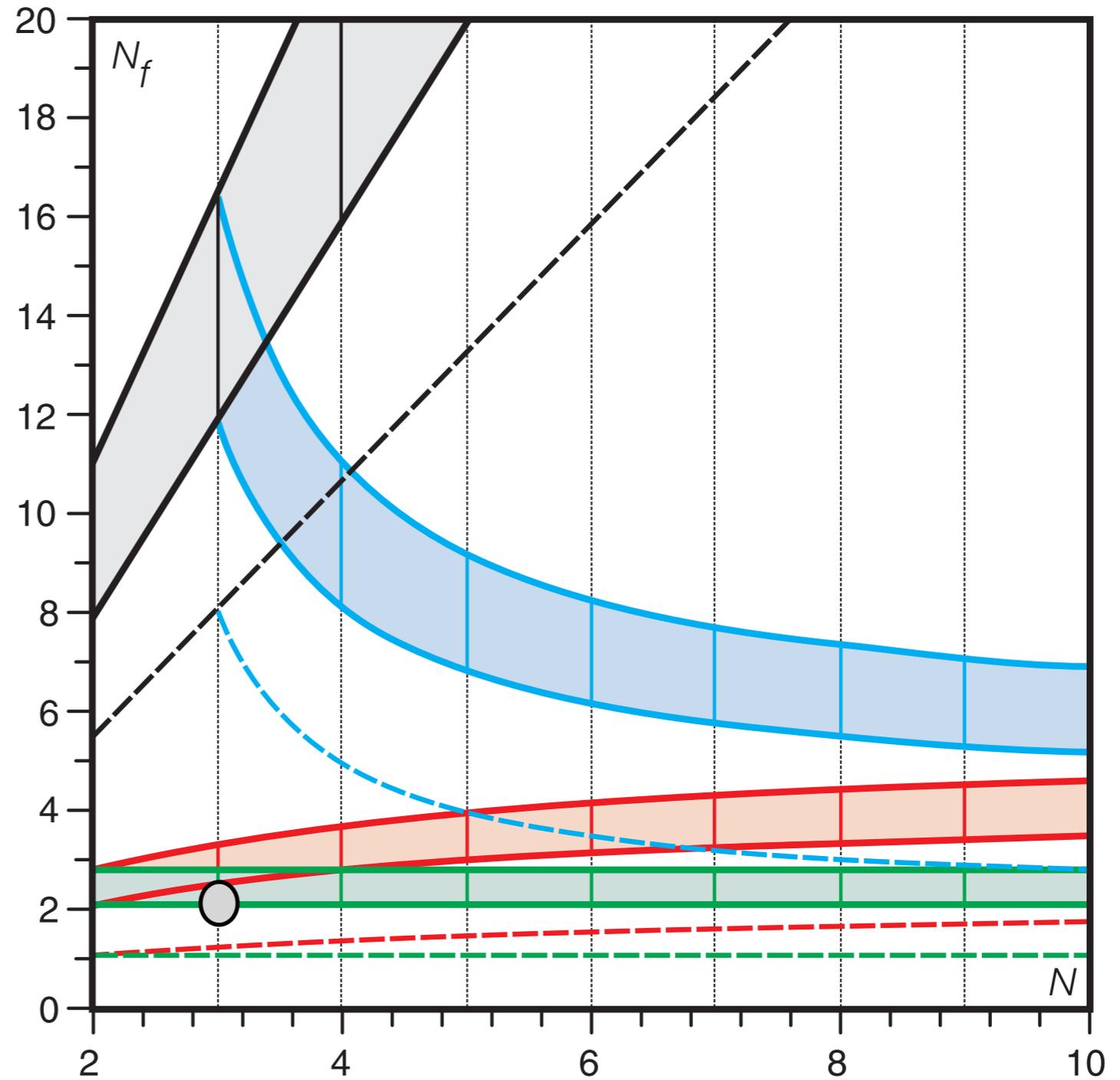
# near-conformal light Higgs (dilaton-like?) sextet rep



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to illustrate: sextet SU(3) color rep

one massless fermion doublet

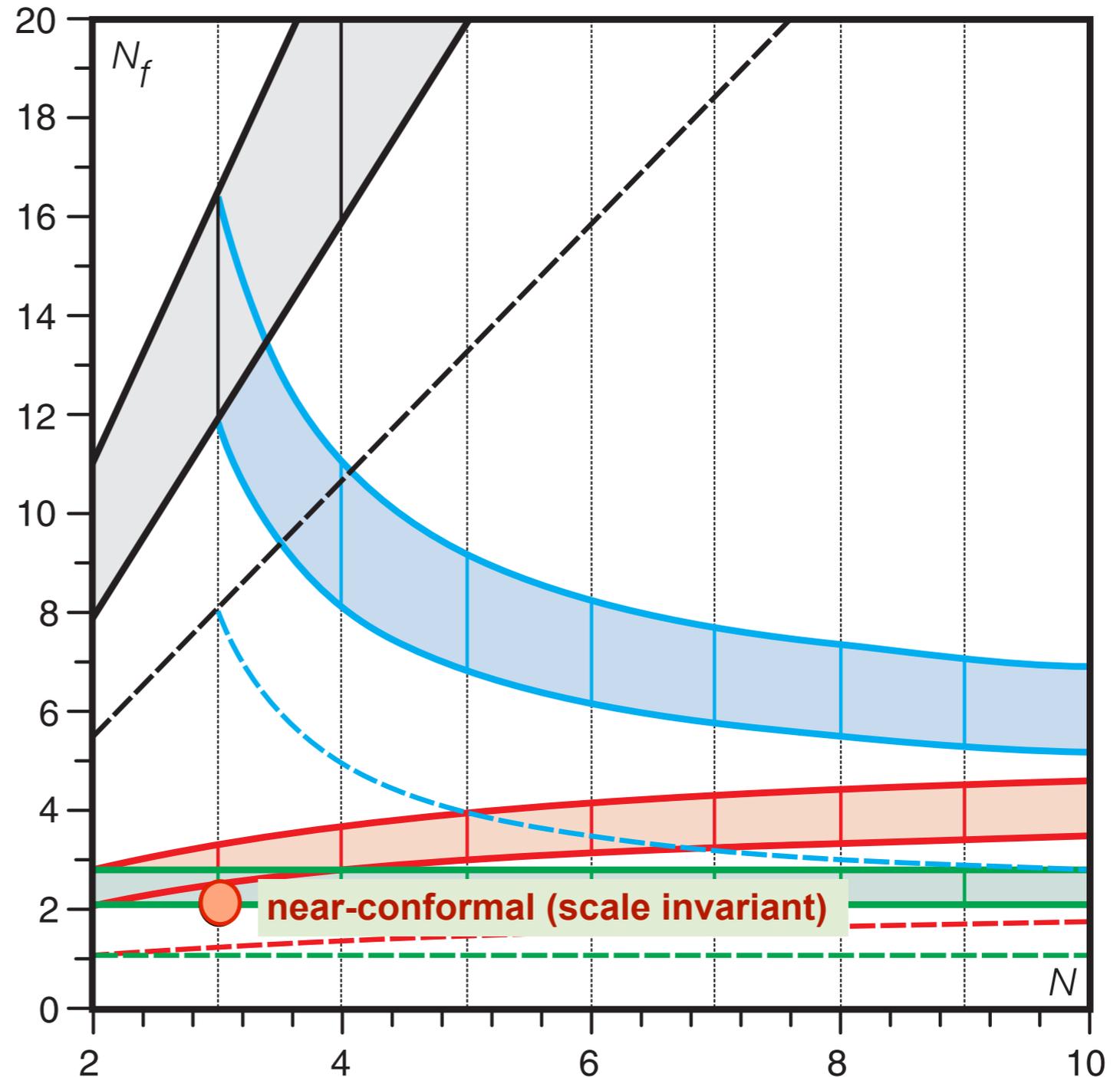
$$\begin{bmatrix} u \\ d \end{bmatrix}$$

$\chi$ SB on  $\Lambda \sim \text{TeV}$  scale

three Goldstone pions  
become longitudinal  
components of weak bosons

composite Higgs mechanism  
scale of Higgs condensate  
 $\sim F=250 \text{ GeV}$

conflicts with EW constraints?



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to apply QCD intuition to near-conformal compositeness is just plain wrong

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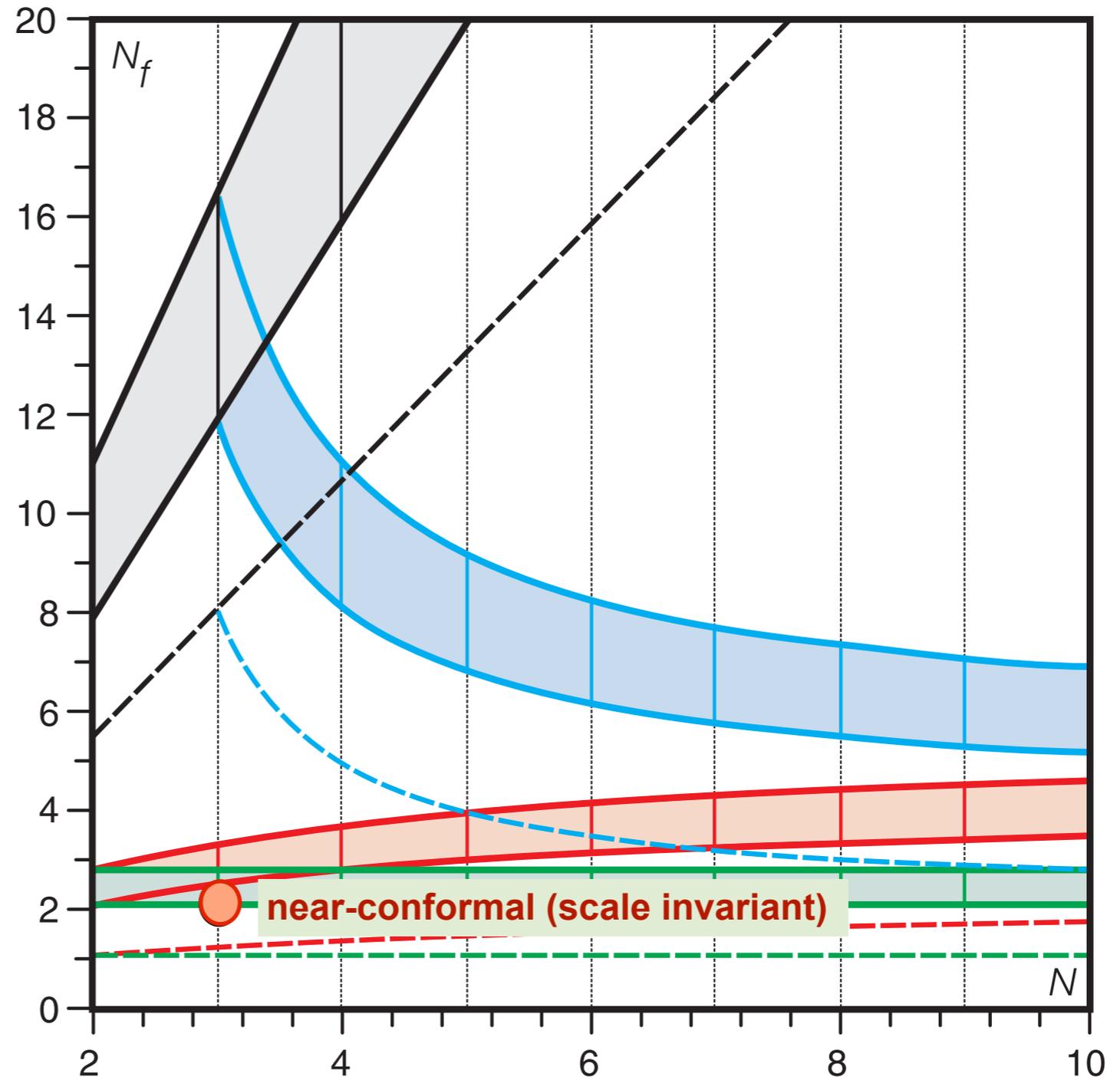
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Technicolor was scaled up QCD too early to worry about new naming rights

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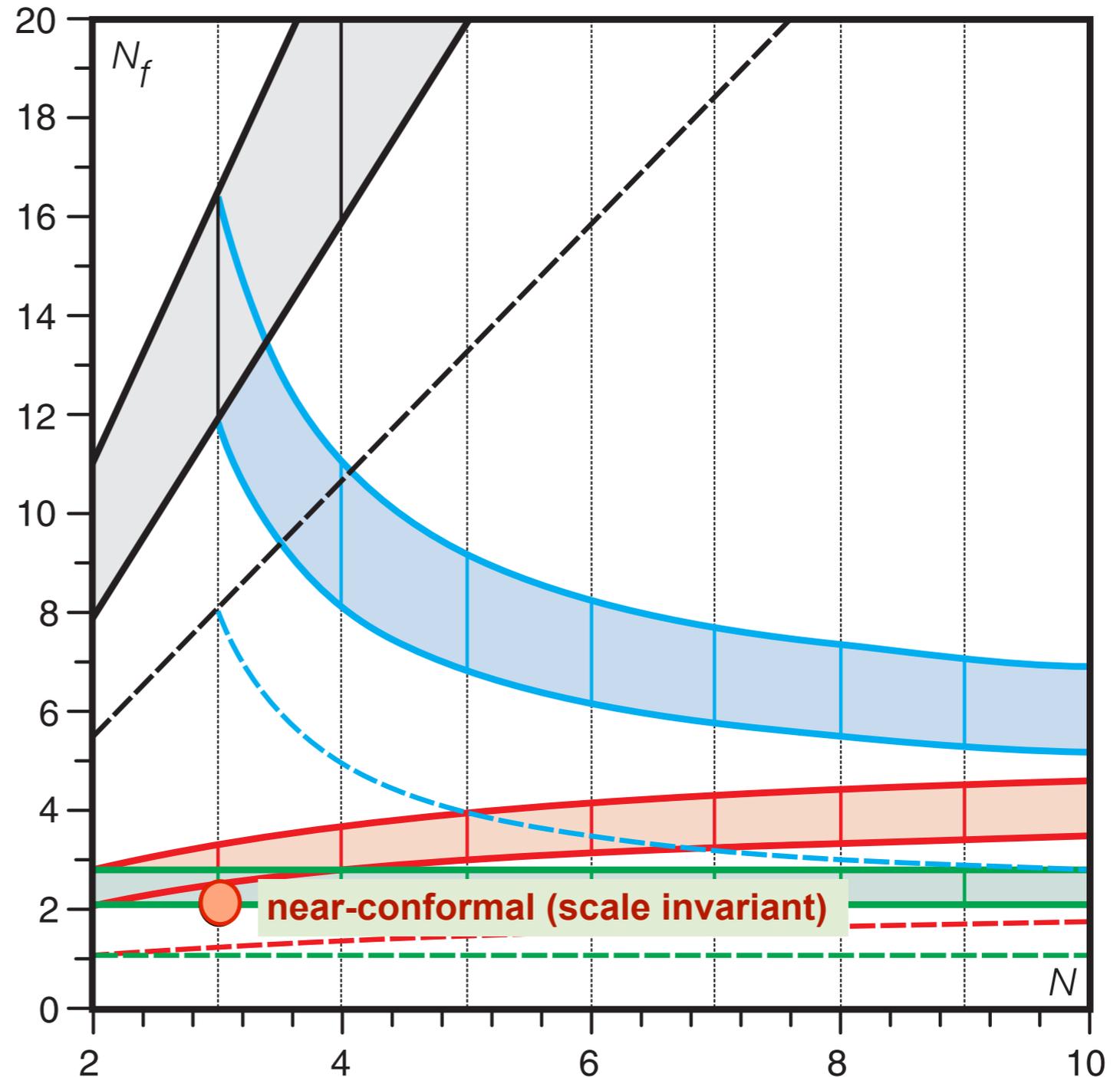
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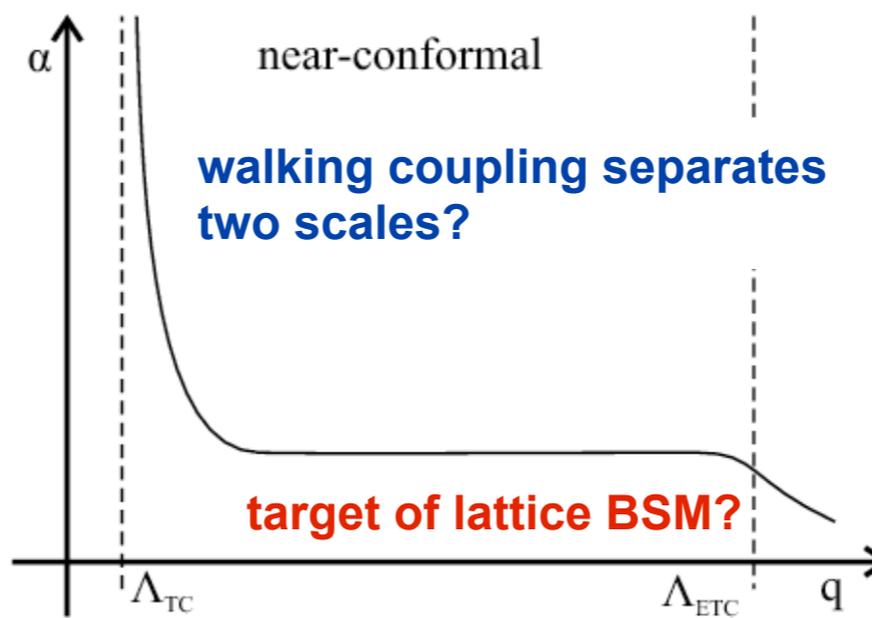
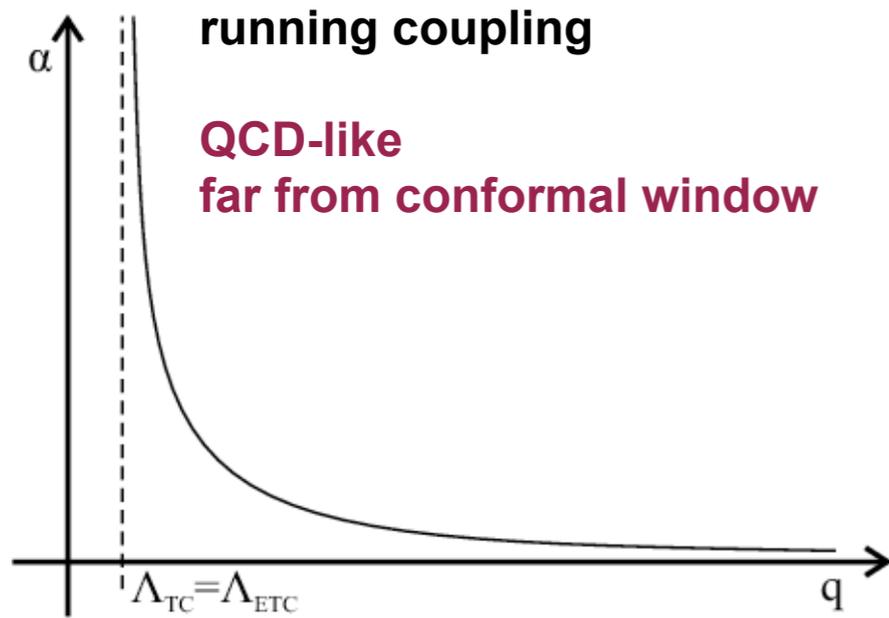
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# light Higgs near conformality (dilaton-like?) sextet



$\chi SB$  on  $\Lambda \sim \text{TeV}$  scale

walking gauge coupling?

fermion mass generation (effective EW int)

composite Higgs mechanism ?

broken scale invariance (dilaton) ?  
or light non-SM composite Higgs  
particle?

Early work using sextet rep:

Marciano (QCD paradigm, 1980)

Kogut, Shigemitsu, Sinclair  
(quenched, 1984)

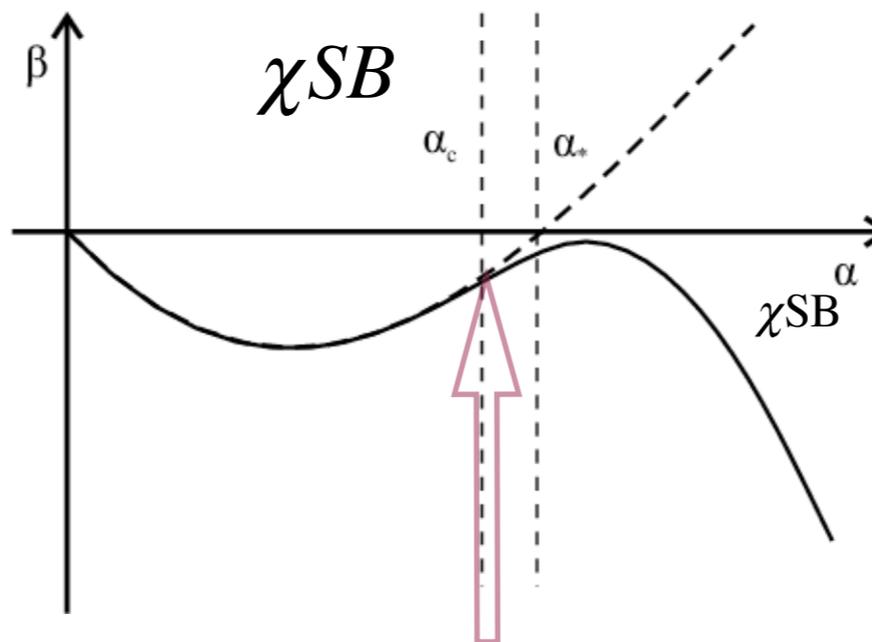
recent work:

Sannino and collaborators

DeGrand, Shamir, Svetitsky  
IRFP or walking gauge coupling

Lattice Higgs Collaboration

Kogut, Sinclair  
finite temperature



when chiral symmetry breaking  
turns conformal FP into walking

to illustrate: sextet SU(3) color rep

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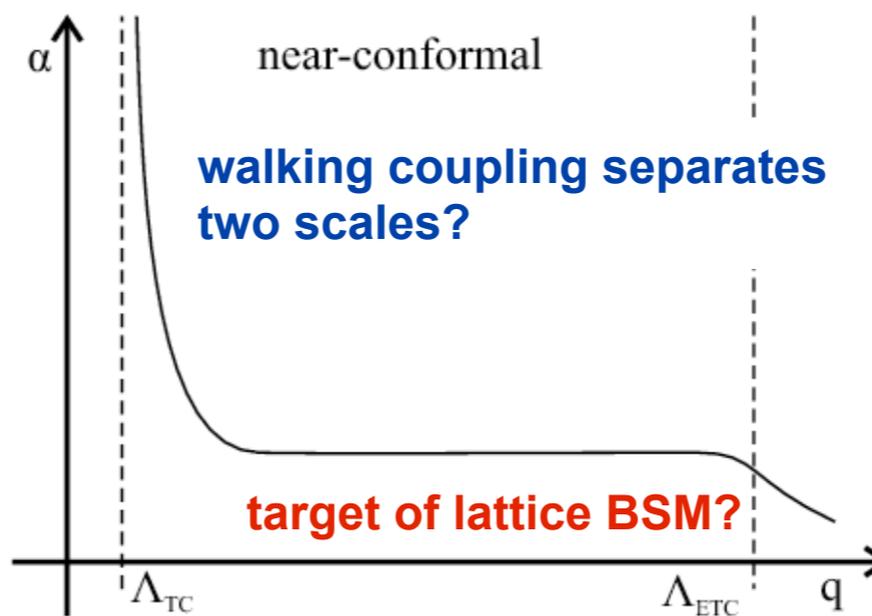
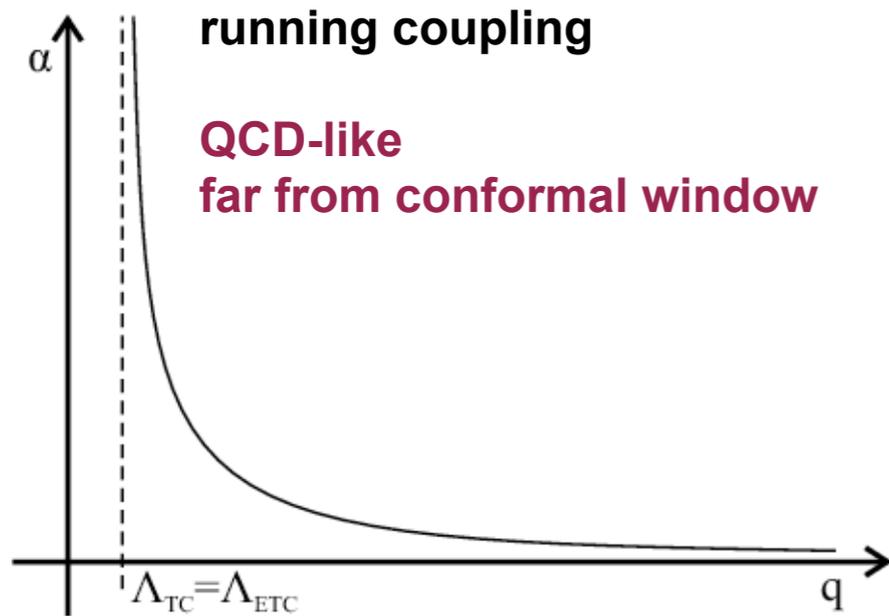
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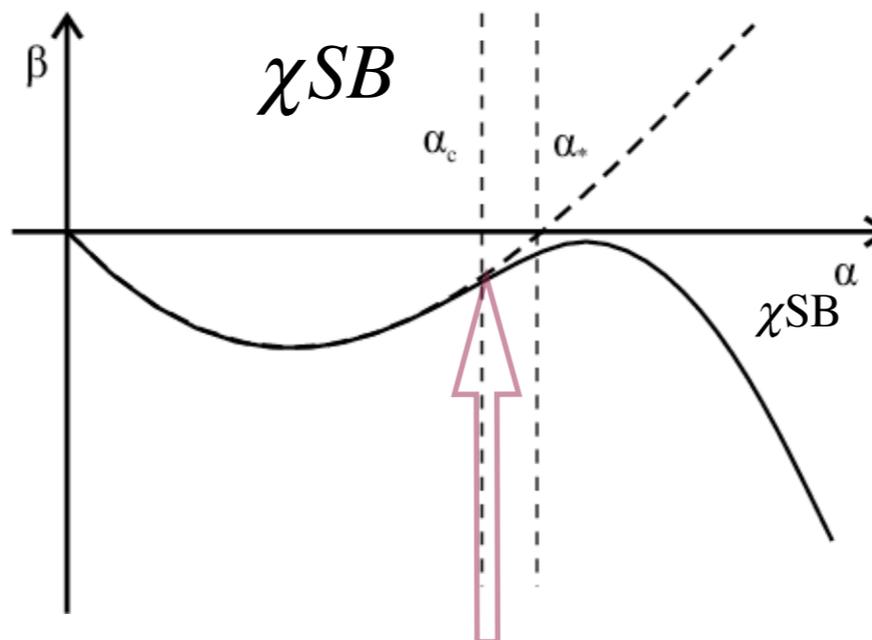
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when chiral symmetry breaking  
turns conformal FP into walking

two expectations:

(1)  $\chi SB$  and confinement

(2) light scalar close to CW (with walking) ?

# light Higgs near conformality (dilaton-like?) sextet

$$m_\sigma^2 \simeq -\frac{4}{f_\sigma^2} \langle 0 | [\Theta_\mu^\mu(0)]_{NP} | 0 \rangle$$

Partially Conserved Dilatation Current (PCDC)

Will gradient flow based technology make the argument less slippery?

$$\partial_\mu \mathcal{D}^\mu = \Theta_\mu^\mu = \frac{\beta(\alpha)}{4\alpha} G_{\mu\nu}^a G^{a\mu\nu}$$

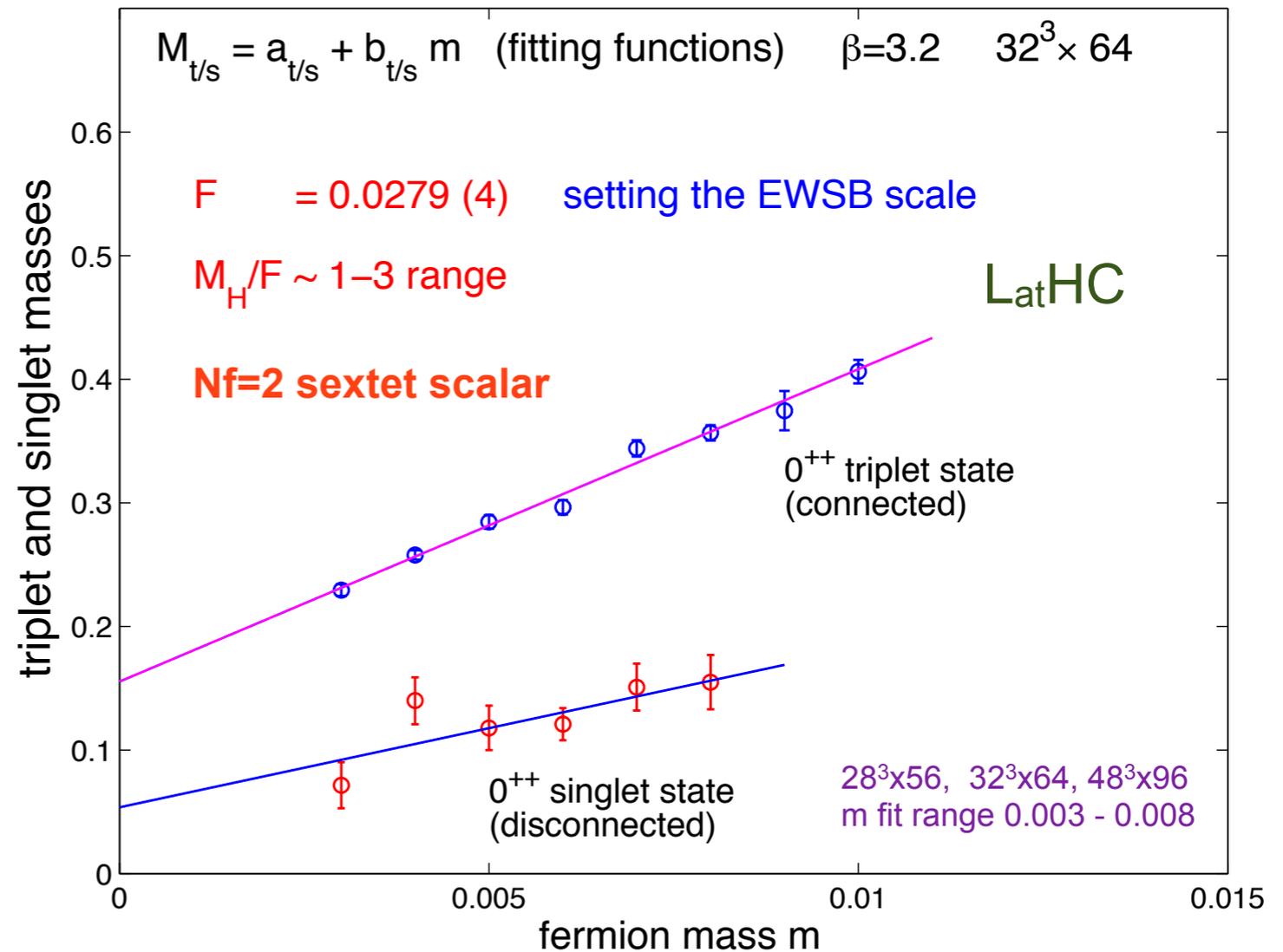
Dilatation current

$$\langle 0 | \Theta^{\mu\nu}(x) | \sigma(p) \rangle = \frac{f_\sigma}{3} (p^\mu p^\nu - g^{\mu\nu} p^2) e^{-ipx}$$

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$$[\Theta_\mu^\mu]_{NP} = \frac{\beta(\alpha)}{4\alpha} [G_{\mu\nu}^a G^{a\mu\nu}]_{NP} \quad \frac{m_\sigma}{f_\sigma} \rightarrow ?$$

Triplet and singlet masses from  $0^{++}$  correlators



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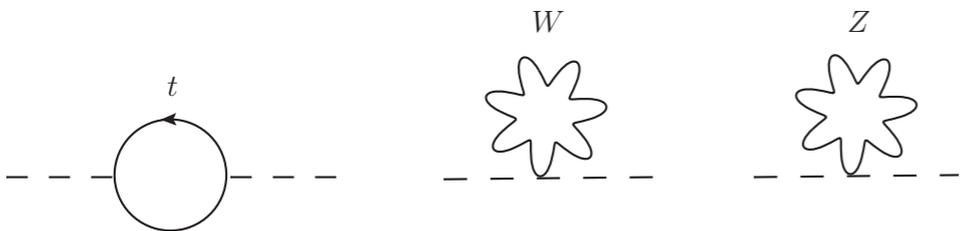
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but how light is light ?

few hundred GeV Higgs impostor?

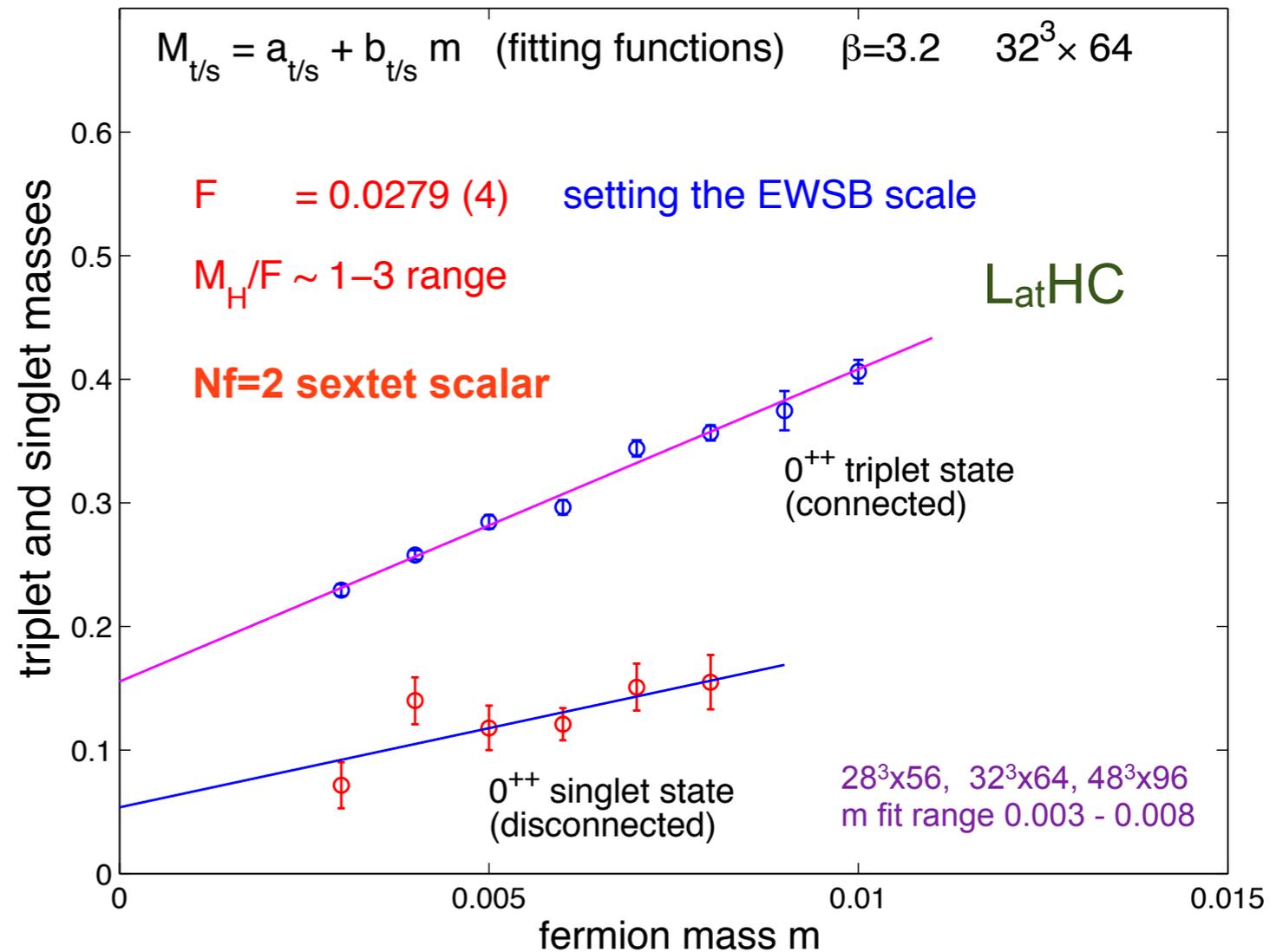
Foadi, Frandsen, Sannino

open for spirited theory discussions



$$\delta M_H^2 \sim -12\kappa^2 r_t^2 m_t^2 \sim -\kappa^2 r_t^2 (600 \text{ GeV})^2$$

Triplet and singlet masses from  $0^{++}$  correlators



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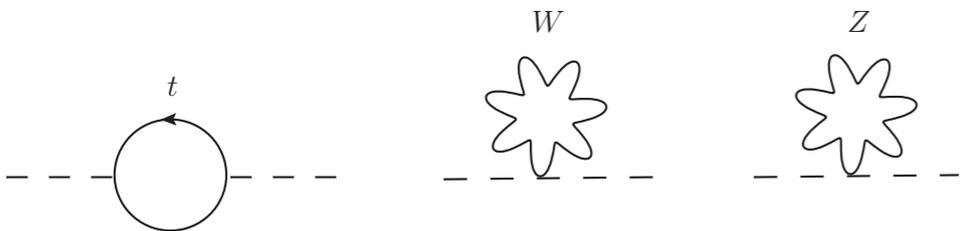
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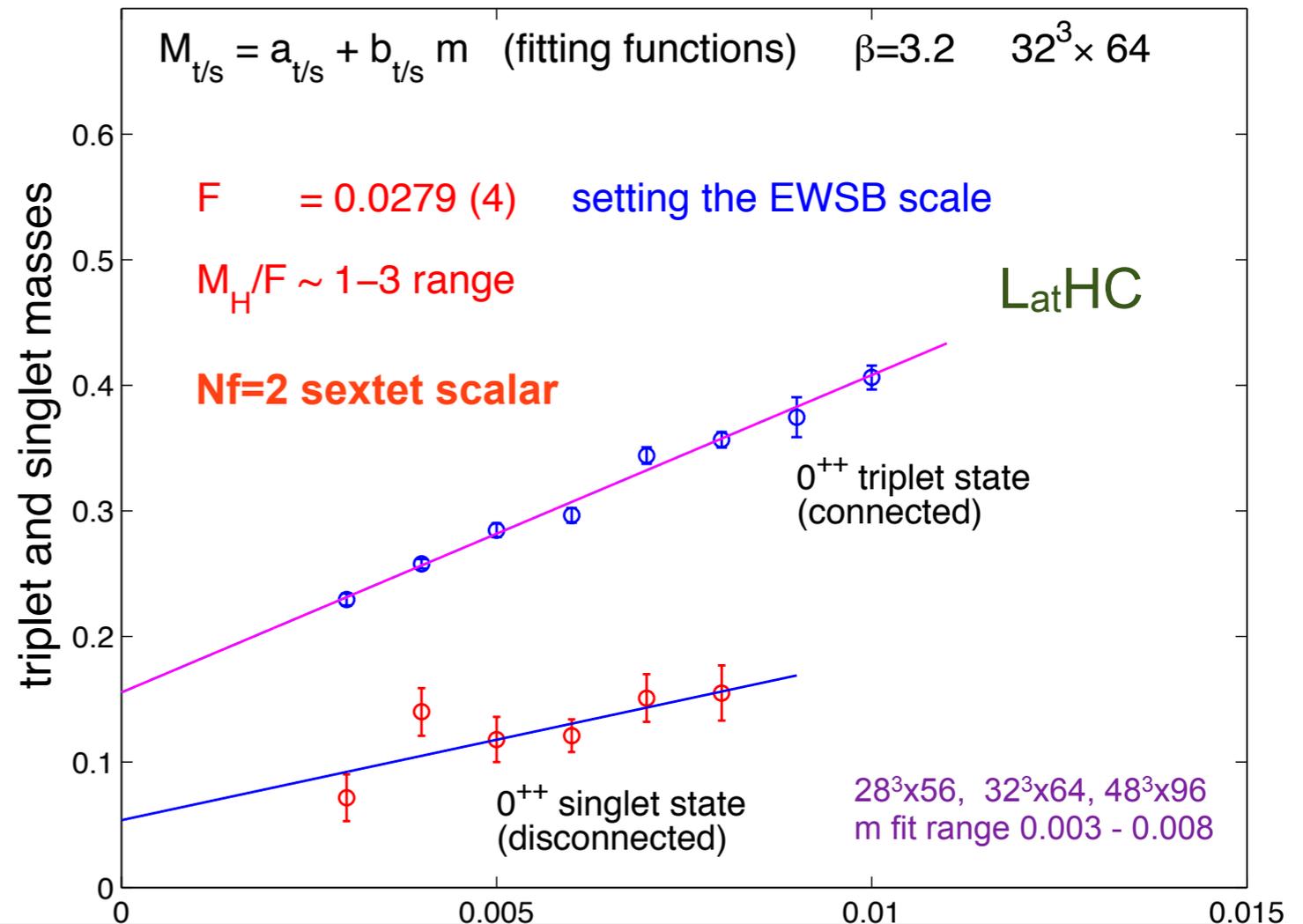
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Triplet and singlet masses from  $0^{++}$  correlators



dilaton-like scalar states in SCGT, or "just a light Higgs" ?

**Our new code (sextet Janos) is highly optimized for BG/Q    impressive Borsanyi/Wong effort  
In Mira production now to answer questions in second generation run set:**

**We started second generation run set  
(ALCC Award on Mira)**

Our new code (sextet Janos) is highly optimized for BG/Q      impressive Borsanyi/Wong effort  
In Mira production now to answer questions in second generation run set:

## 1. Test of chiral perturbation theory below the scale of low mass scalar?

how to test if light scalar is dilaton-like

close to CW?

both require new low energy effective action

is there an  $f_\sigma/f_\pi$  crisis?

## 2. Needs precise scale setting and resonance spectrum

S and T parameters of Electroweak precision tests

large volumes  $F \cdot L \sim 1$ , or larger!

slow topology

We started second generation run set  
(ALCC Award on Mira)

## 3. Running (walking?) coupling

volume-dependent running coupling

scale-dependent  $L = \infty$  coupling in chiral limit

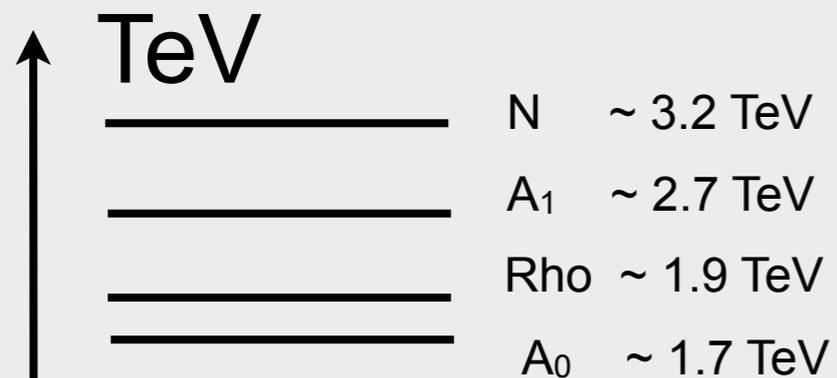
## 4. Consistent chiral condensate?

GMOR relation is important consistency check

new method for spectral density and mode number

anomalous dimension of chiral condensate

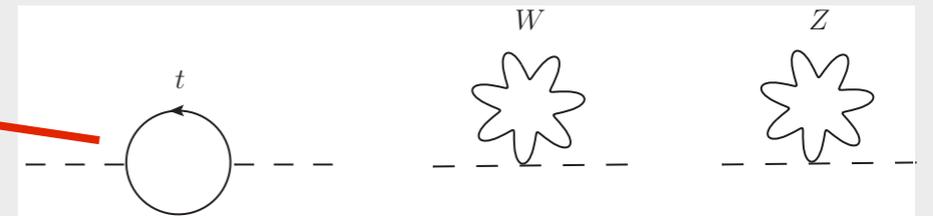
# the spectrum



near-conformal resonance spectrum  
separated from light scalar

within LHC14 reach

— scalar impostor few hundred GeV?  
— EW self-energy shift  
— observed Higgs-like?



$$\delta M_H^2 \sim -12\kappa^2 r_t^2 m_t^2 \sim -\kappa^2 r_t^2 (600 \text{ GeV})^2$$

# light composite Higgs and EW constraints

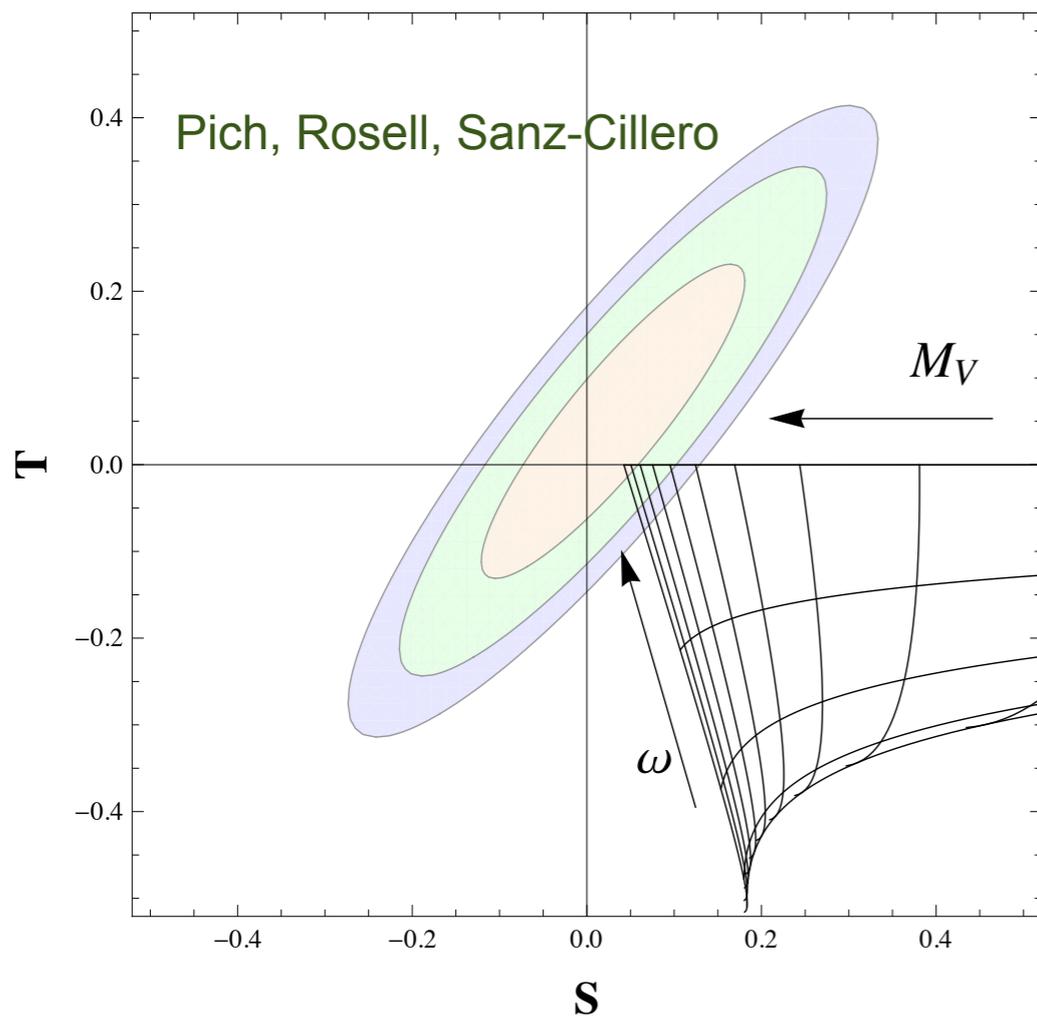


FIG. 2. NLO determinations of  $S$  and  $T$ , imposing the two WSRs. The approximately vertical curves correspond to constant values of  $M_V$ , from 1.5 to 6.0 TeV at intervals of 0.5 TeV. The approximately horizontal curves have constant values of  $\omega$ : 0.00, 0.25, 0.50, 0.75, 1.00. The arrows indicate the directions of growing  $M_V$  and  $\omega$ . The ellipses give the experimentally allowed regions at 68% (orange), 95% (green) and 99% (blue) CL.

$$S = \frac{16\pi}{g^2 \tan \theta_W} \int_0^\infty \frac{dt}{t} [\rho_S(t) - \rho_S(t)^{\text{SM}}]$$

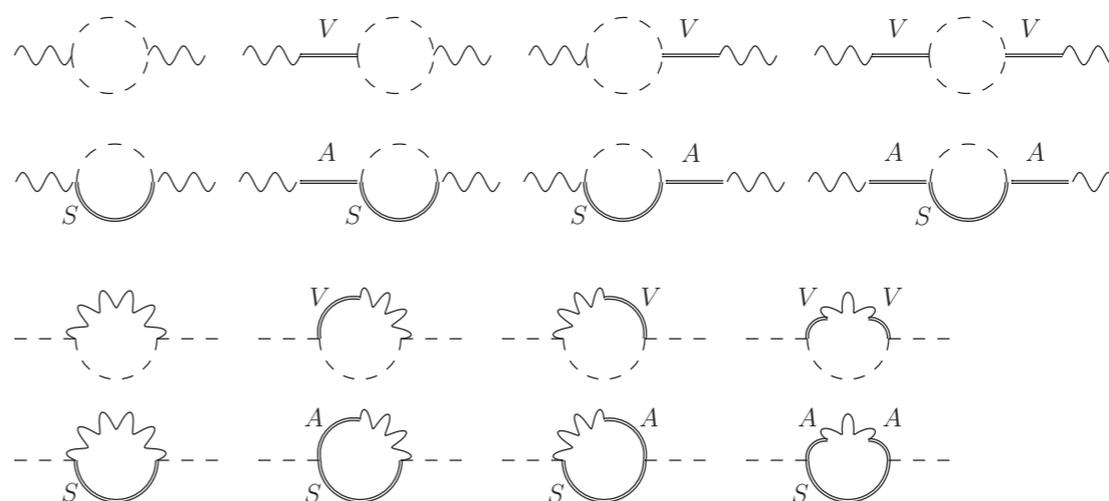
$$S_{\text{LO}} = 4\pi \left( \frac{F_V^2}{M_V^2} - \frac{F_A^2}{M_A^2} \right)$$

$$T = \frac{4\pi}{g'^2 \cos^2 \theta_W} \int_0^\infty \frac{dt}{t^2} [\rho_T(t) - \rho_T(t)^{\text{SM}}]$$

From two Weinberg sum rules and from NLO loop expansion:

$M_V, M_A \sim 2$  TeV or higher is compatible with  $S, T$  constraints (it is tight and arguably ambiguous)

more work needed



**NLO S-param**

$$S = 0.03 \pm 0.10$$

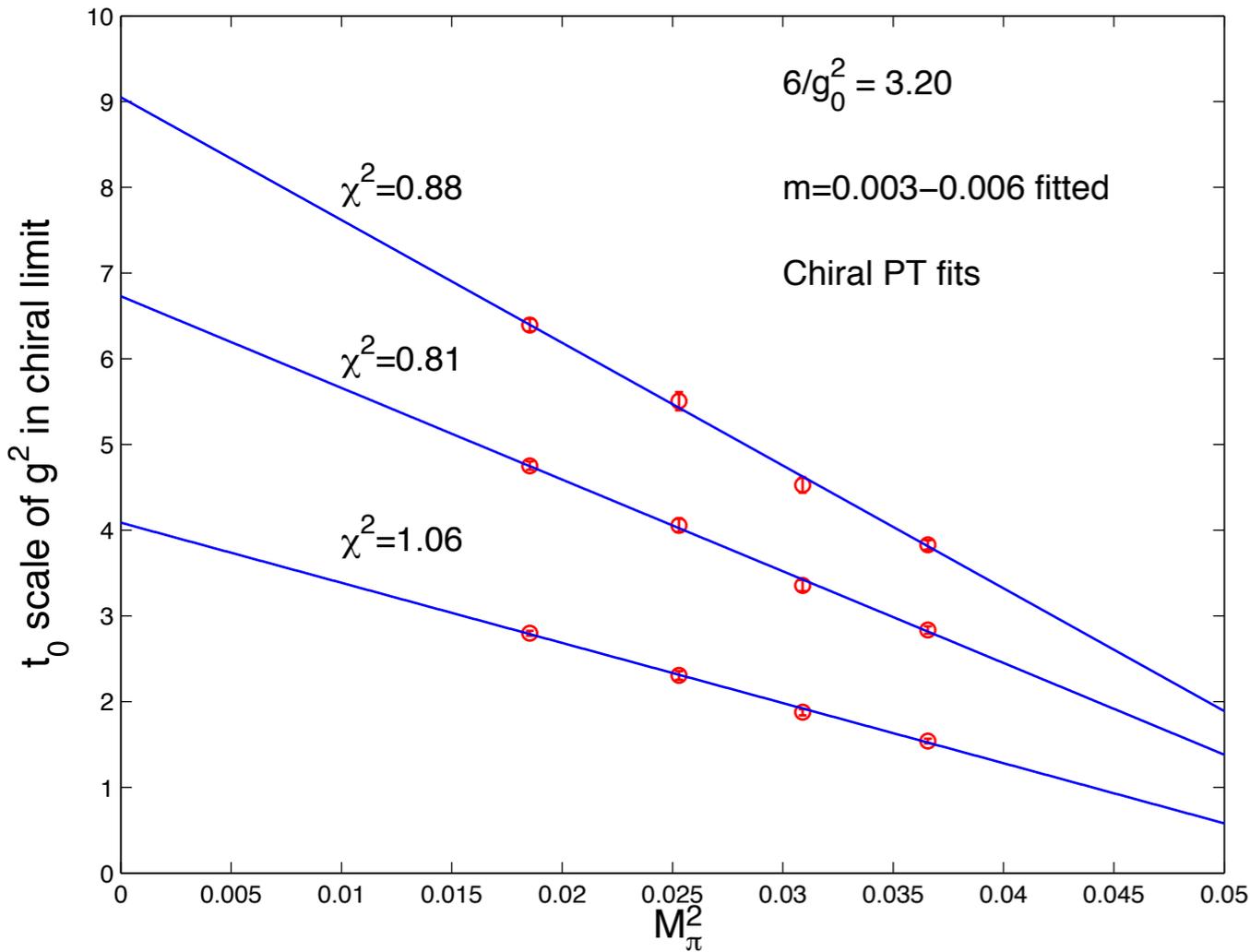
**global fits**

**NLO T-param**

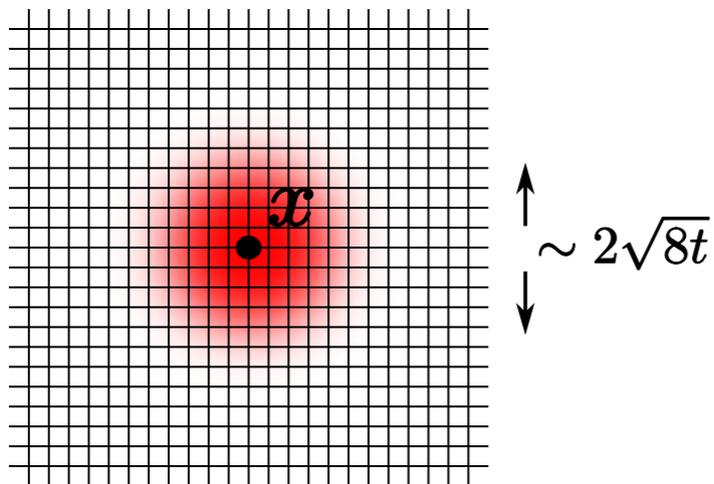
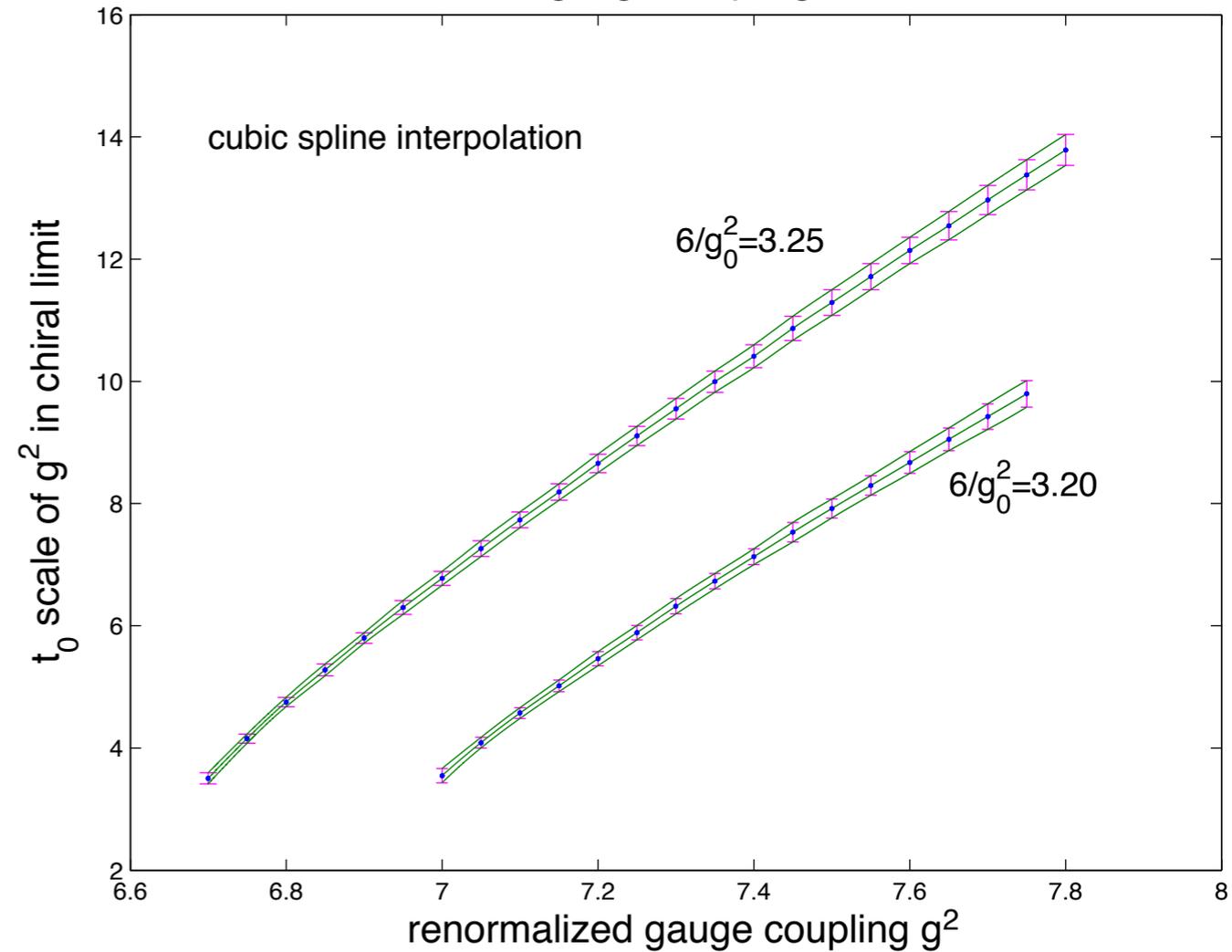
$$T = 0.05 \pm 0.12$$

# gradient flow and gauge dependent renormalized coupling in chiral limit

$t_0$  scale of selected  $g^2$  series in  $m=0$  chiral limit



renormalized gauge coupling in chiral limit



$$\langle t^2 E(t) \rangle = g_0^2 t^2 \int_{-\frac{\pi}{a}}^{\frac{\pi}{a}} \frac{d^4 p}{(2\pi)^4} \text{Tr} \left( e^{-t(S^f + \mathcal{G})} (\mathcal{S}^g + \mathcal{G})^{-1} e^{-t(S^f + \mathcal{G})} \mathcal{S}^e \right)$$

We presented to scale dependent running coupling methods at Lattice 2014 both are gradient flow based

# The chiral condensate in the sextet model

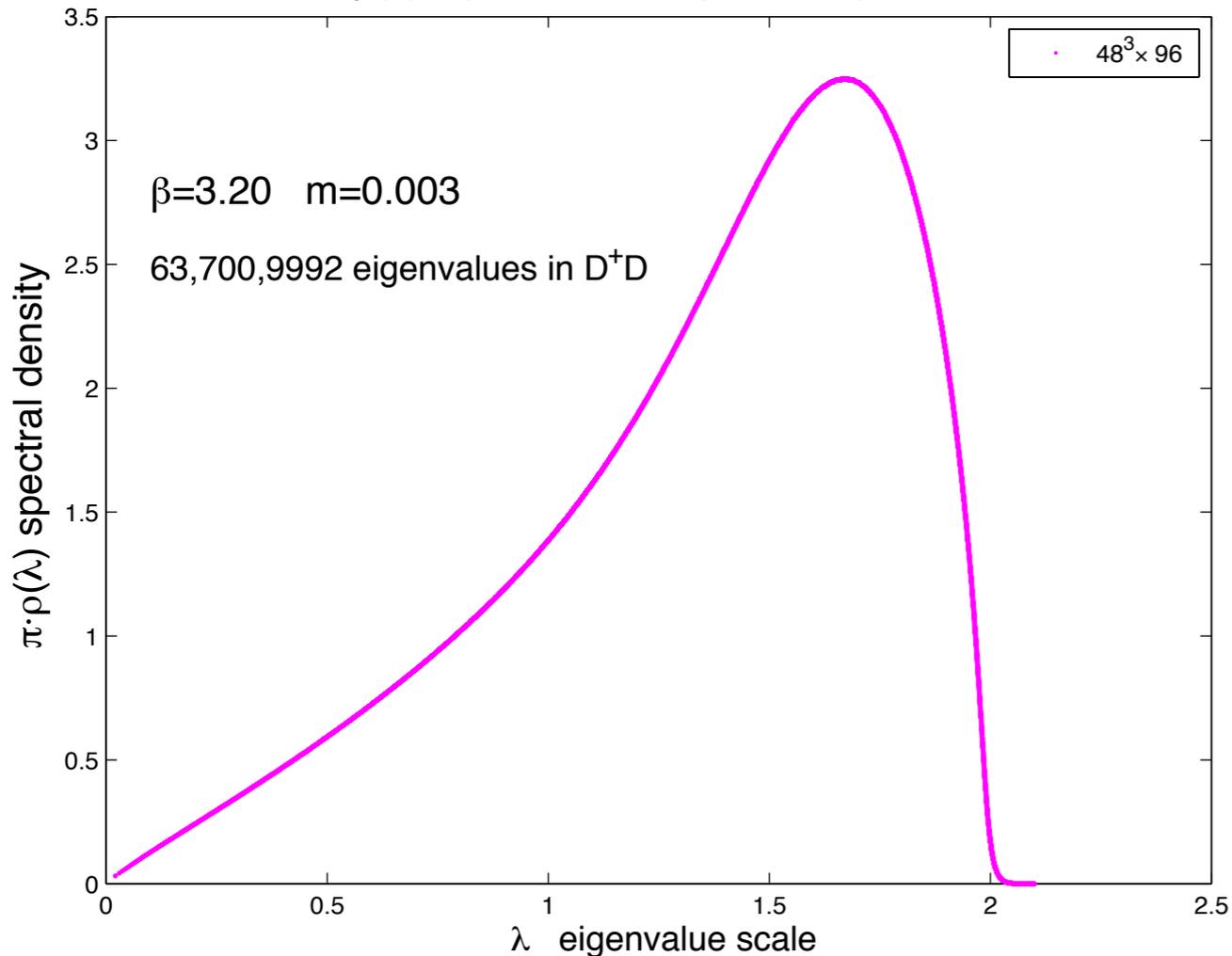
new stochastic method **sextet Nf=2**

direct determination of full spectral density and mode number distribution on gauge configurations

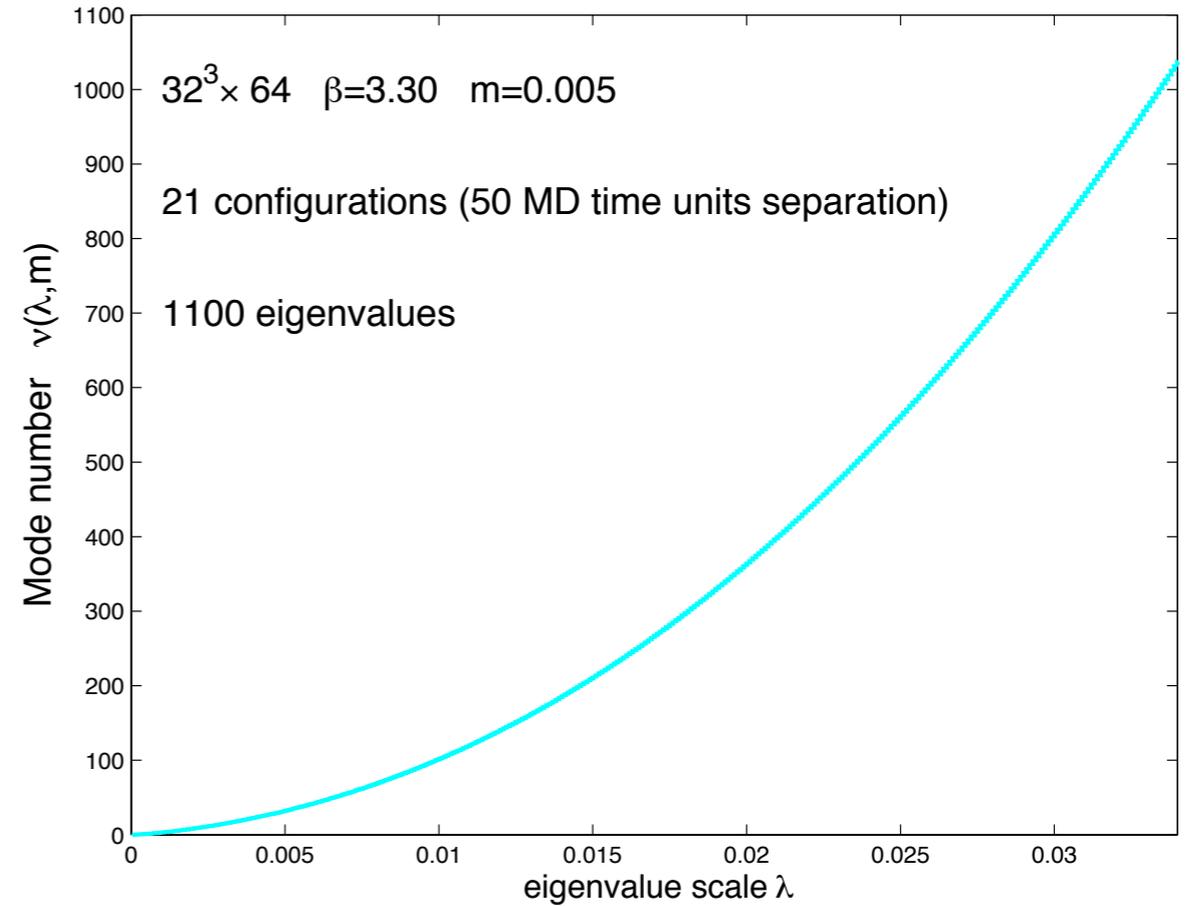
passed all tests so far  
scale-dependent determination of the anomalous dimension of the chiral condensate

deployed now in our RMT and crossover regime studies of the condensate (Damgaard, Fukaya, Aoki et al.)

$\pi \cdot \rho(\lambda)$  spectral density of full spectrum



Scale dependence of Mode number distribution  $v(\lambda, n)$



# The chiral condensate in the sextet model

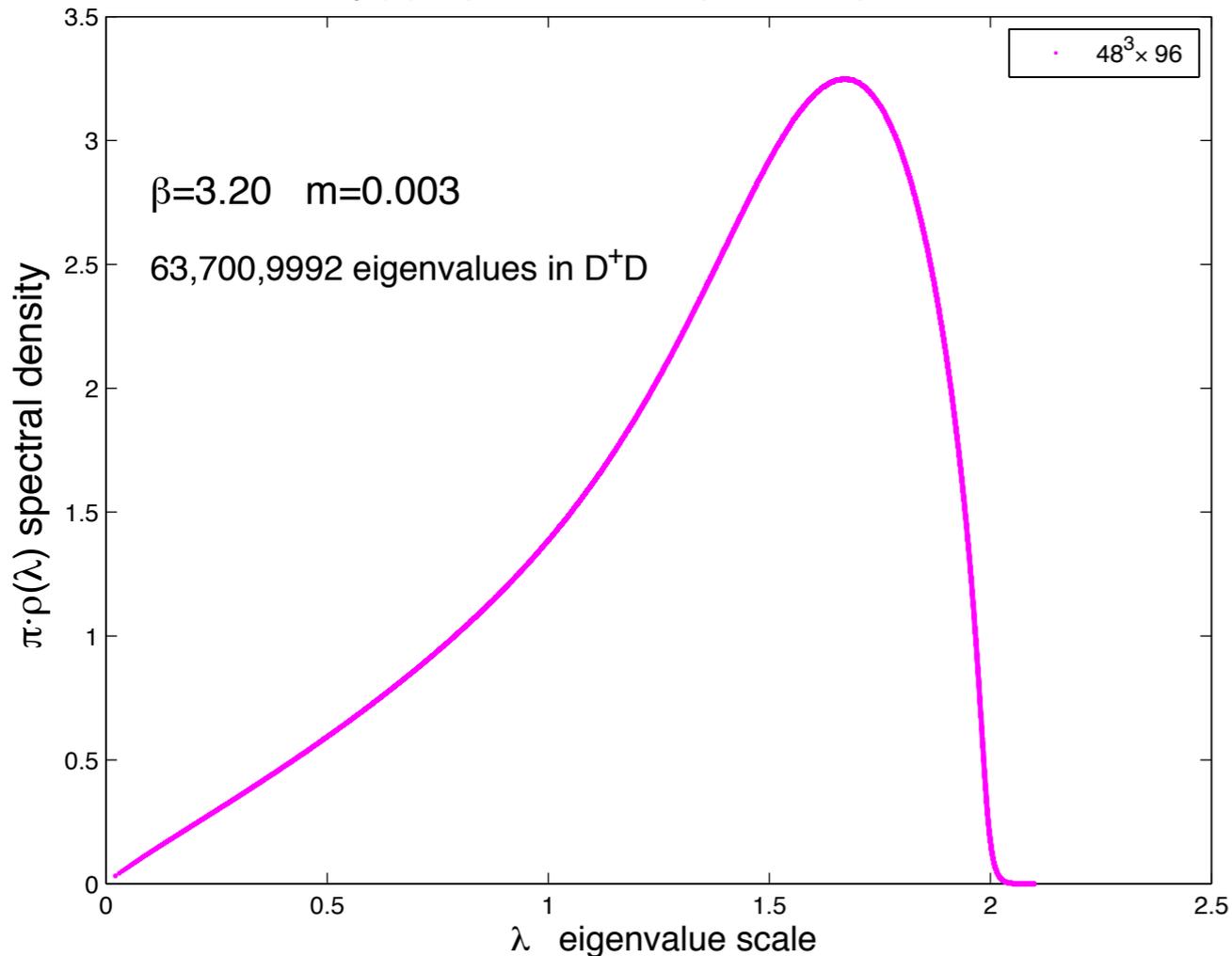
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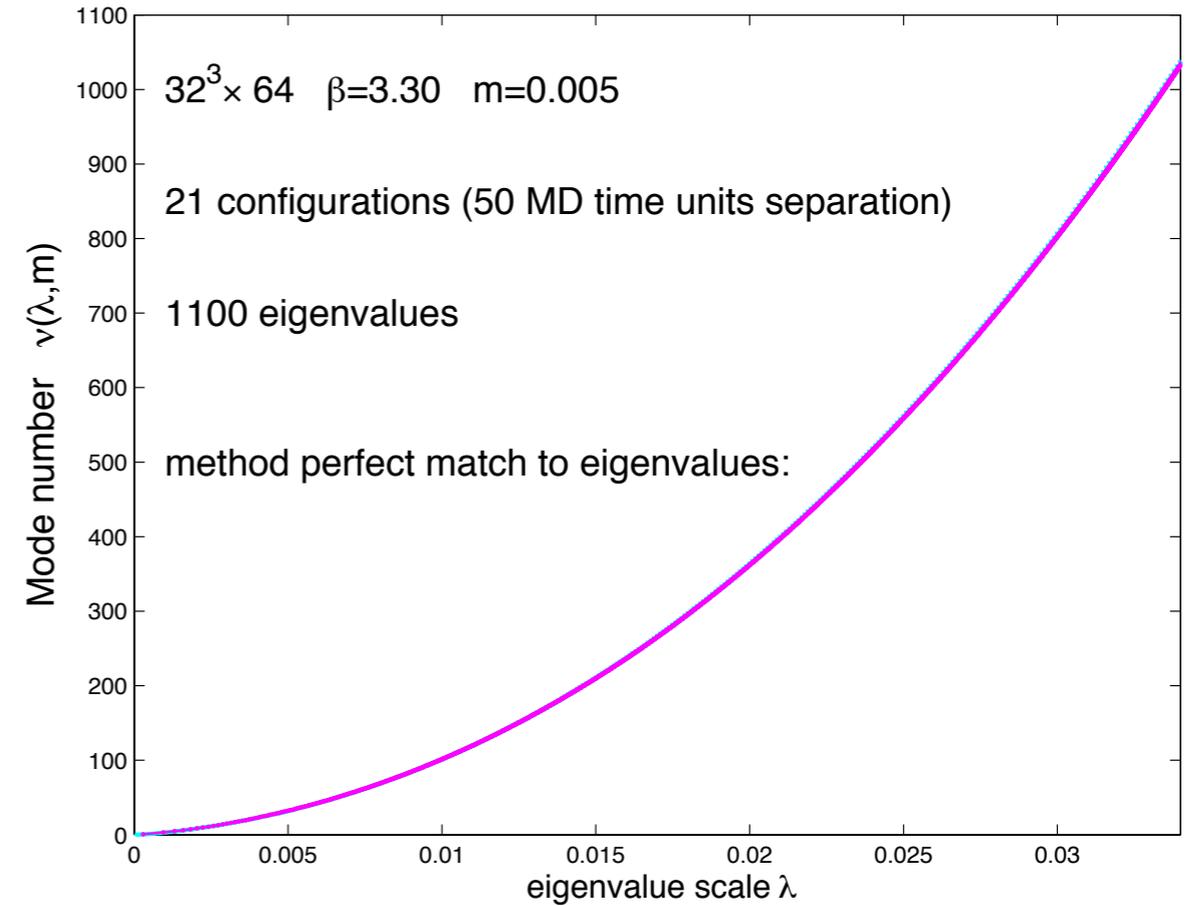
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Scale dependence of Mode number distribution  $v(\lambda, n)$



# Early universe and the sextet model?

Kogut-Sinclair work consistent with finite temperature  $\chi$ SB phase transition  
 Relevance in early cosmology? (order of the phase transition?)

The Total Energy of the Universe:

Vacuum Energy (Dark Energy)  $\sim 67\%$

Dark Matter  $\sim 29\%$

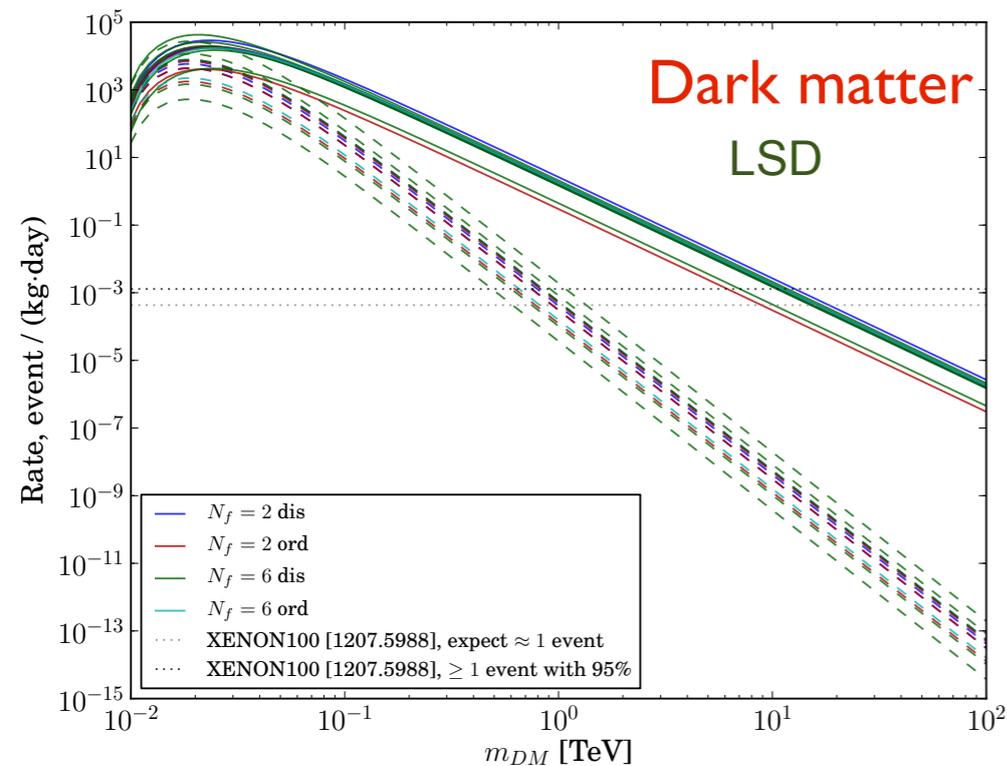
Visible Baryonic Matter  $\sim 4\%$

**Dark matter**

self-interacting?

O(barn) cross section would be challenging

T. Appelquist, R. C. Brower, M. I. Buchoff, M. Cheng, S. D. Cohen, G. T. Fleming, J. Kiskis, M. F. Lin, E. T. Neil, J. C. Osborn, C. Rebbi, D. Schaich, C. Schroeder, S. Syritsyn, G. Voronov, P. Vranas, and J. Wasem (Lattice Strong Dynamics (LSD) Collaboration)



- lattice BSM phenomenology of dark matter pioneering LSD work

- $N_f=2$   $Q_u=2/3$   $Q_d = -1/3$  udd neutral dark matter candidate

- dark matter candidate **sextet  $N_f=2$**  electroweak active in the application

- there is room for third heavy fermion flavor as electroweak singlet

- rather subtle sextet baryon  **$\sim 3$  TeV** construction (symmetric in color)

# Summary and Outlook

## Simplest composite scalar is light near conformality

light scalar (dilaton-like?) emerging

close to conformal window?

running (walking) coupling in progress

gradient flow deployed

chiral condensate

new method is promising

spectroscopy

emerging resonance spectrum  $\sim 2\text{-}3\text{ TeV}$

dark matter

implications are intriguing  
strong self-interactions?

Tuning with third flavor ?

We have a candidate for the minimal Higgs impostor

Can we make it fail?

**Congratulations and best wishes Mike!**

**We will need your wise council in the future!**